

Wednesday 12/4/19

1. Grab Notes/Calculator
2. Take out HW/Calendar
3. Begin Warm-up
4. Rational Root Theorem Notes

**Topic:** Rational Root Theorem

**Name:** \_\_\_\_\_

**What am I learning today?**

**Warm-Up:**

Prove the zeros of the polynomial with synthetic division. Then find the remaining zero(s) using the result.

1.  $f(x) = 2x^3 - 3x^2 - 32x - 15; x = -\frac{1}{2}, x = 5$

2.  $3x^3 - 3x^2 - 5x + 5; x = 1$

$2x + 6 = 0$   
 $2x = -6$   
 $x = -3$

$(x - 1)(3x^2 - 5)$

$3x^2 - 5 = 0$   
 $3x^2 = 5$   
 $x^2 = \frac{5}{3}$   
 $x = \pm\sqrt{\frac{5}{3}}$

**Vocabulary**

Rational Root Theorem

The **Rational Root Thm.** provides a complete list of all possible rational roots of a polynomial equation.

To find all possible rational roots, do the following:

$\pm \frac{C}{L} = \pm \frac{\text{factors of the constant term}}{\text{factors of the leading coefficient}}$

Ex. 1: Find/list all the possible rational roots of the following polynomials.

a.  $f(x) = 3x^3 - 3x^2 + 15x - 40$

$C(40): 4, 10, 20, 2, 5, 8, 1, 40$   
 $L(3): 1, 3$   
**PRR:**  $\pm 4, \pm \frac{4}{3}, \pm 10, \pm \frac{10}{3}, \pm 20, \pm \frac{20}{3}, \dots$

b.  $f(x) = -15x^4 + 3x^3 - 9x^2 - x + 24$

$C(24): 1, 24, 2, 12, 4, 6, 8, 3$   
 $L(-15): 5, 3, 1, 15$   
**PRR:**  $\pm \frac{1}{3}, \pm \frac{1}{5}, \pm 1, \pm \frac{1}{15}, \pm \frac{24}{3}, \pm 8, \pm 24, \pm \frac{8}{5}, \dots$

**Recall**

Writing Zeros as Factors

Recall from a previous unit how we wrote zeros as factors so we could write a polynomial in factored form.

Ex. 2: Write the following zeros/roots/x-intercepts as a polynomial in factored form.

a.  $x = \frac{2}{3}, x = -4, x = 3$

$3x = 2$   
 $3x - 2 = 0$

$x = -4$   
 $x + 4$

$x = 3$   
 $x - 3$

$f(x) = (3x - 2)(x + 4)(x - 3)$

b.  $x = 0, x = -\frac{5}{2}, x = -2, x = 1$

$2x = -5$   
 $2x + 5 = 0$

$x = -2$   
 $x + 2 = 0$

$x = 1$   
 $x - 1 = 0$

$f(x) = (x)(2x + 5)(x + 2)(x - 1)$

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**Steps**

Finding All Zeros and Writing in Factored Form

Steps to find the zeros of a polynomial and use the zeros to write the polynomial in factored form:

1. Find/list all the possible rational roots ( $\pm \frac{c}{l}$ )
2. Use the calculator to find the rational roots (see steps below)
3. Prove the zeros from the calculator are zeros/roots using synthetic division.
4. Solve for any missing zeros (using the last line from synthetic division).
5. Use found zeros to write in factored form.

**CALCULATOR STEPS:**

1. Press **table**, select **Edit Function**, enter a functions and press **enter**.
2. Select **Table Start** and **Table Step** values, then hit **CALC**.

**Example**

$C(15): 1, 15, 3, 5$   
 $L(1): 1$

Ex. 3: List all possible rational roots. Then use a calculator, synthetic division and factoring to find all zeros & write in factored form (no fractions).

$f(x) = x^3 - x^2 - 17x - 15$

PRR:  $\pm 1, \pm 15, \pm 3, \pm 5$

Zeros:  $x = -1, x = -3, x = 5$

Factored Form:  $(x+1)(x+3)(x-5)$

$f(x) = (x+1)(x+3)(x-5)$

$$\begin{array}{r|rrrr} -1 & 1 & -1 & -17 & -15 \\ & \downarrow & -1 & 2 & 15 \\ -3 & & -2 & -15 & 0 \\ & \downarrow & -3 & 15 & \\ 5 & & 5 & 0 & \\ \hline & 1 & 0 & & \end{array}$$

**Example**

$C(15): 5, 3, 1, 15$   
 $L(2): 1, 2$

Ex. 4: List all possible rational roots. Then use a calculator, synthetic division and factoring to find all zeros & write in factored form (no fractions).

$f(x) = 2x^4 + 11x^3 + 13x^2 - 11x - 15$

PRR:  $\pm 5, \pm \frac{5}{2}, \pm 3, \pm \frac{3}{2}, \pm 1, \pm \frac{1}{2}$   
 $\pm 15, \pm \frac{15}{2}$

Zeros:  $x = 1, x = -3, x = -1, x = -\frac{5}{2}$

Factored Form:

$f(x) = (x-1)(x+3)(x+1)(2x+5)$

$$\begin{array}{r|rrrrr} 1 & 2 & 11 & 13 & -11 & -15 \\ & \downarrow & 13 & 26 & 15 & 0 \\ -3 & & -6 & -21 & -15 & 0 \\ & \downarrow & -7 & -5 & 0 & \\ -1 & & -2 & -5 & 0 & \\ \hline & 2 & 9 & 0 & & \end{array}$$

$2x + 5 = 0$   
 $2x = -5$   
 $x = -\frac{5}{2}$

**You Try**

Ex. 5: List all possible rational roots. Then use a calculator, synthetic division and factoring to find all zeros & write in factored form (no fractions).

$f(x) = 5x^3 + 2x^2 - 45x - 18$

PRR:

Zeros: \_\_\_\_\_

Factored Form:

$f(x) =$  \_\_\_\_\_