

Use the remainder theorem (direct substitution) and synthetic division to determine whether the given value is a zero of the polynomial. Be sure to include your conclusion statement.

1.  $f(x) = -2x^3 + 4x^2 - 6x$

a.)  $f(-1) = -2(-1)^3 + 4(-1)^2 - 6(-1)$

$$-1 \begin{array}{r|rrrr} -2 & 4 & -6 & 0 \\ \downarrow & & & & \\ -2 & 6 & -12 & 12 \end{array}$$

\* No,  $x = -1$  is NOT a zero.

b.)  $f(0) = -2(0)^3 + 4(0)^2 - 6(0)$

$$0 \begin{array}{r|rrrr} -2 & 4 & -6 & 0 \\ \downarrow & & & & \\ -2 & 4 & -6 & 0 \end{array}$$

\* Yes,  $x = 0$  is a zero.

2.  $f(x) = 2x^3 + 7x^2 + 2x - 3$

a.)  $f(0) = 2(0)^3 + 7(0)^2 + 2(0) - 3$

$$0 \begin{array}{r|rrrr} 2 & 7 & 2 & -3 \\ \downarrow & & & & \\ 2 & 7 & 2 & -3 \end{array}$$

\* No,  $x = 0$  is NOT a zero.

b.)  $f(\frac{1}{2}) = 2(\frac{1}{2})^3 + 7(\frac{1}{2})^2 + 2(\frac{1}{2}) - 3$

$$\frac{1}{2} \begin{array}{r|rrrr} 2 & 7 & 2 & -3 \\ \downarrow & & & & \\ 2 & 8 & 6 & 0 \end{array}$$

\* Yes,  $x = \frac{1}{2}$  is a zero.

Given the following functions and x-intercepts find the remaining zero.

3.  $f(x) = x^3 - 3x^2 - 10x + 24$ ;  $-3, 4, 2$

$$-3 \begin{array}{r|rrrr} 1 & -3 & -10 & 24 \\ \downarrow & & & & \\ 1 & -6 & 8 & 0 \\ \downarrow & & & & \\ 1 & -2 & 0 & \end{array}$$

$x - 2 = 0$   
 $x = 2$

4.  $f(x) = 6x^3 - x^2 - 5x + 2$ ;  $-1, \frac{1}{2}, \frac{2}{3}$

$$-1 \begin{array}{r|rrrr} 6 & -1 & -5 & 2 \\ \downarrow & & & & \\ 6 & -6 & 7 & -2 \\ \downarrow & & & & \\ 6 & -7 & 2 & 0 \\ \downarrow & & & & \\ 6 & -4 & 0 & \end{array}$$

$6x - 4 = 0$   
 $6x = 4$

$x = \frac{4}{6} = \frac{2}{3}$

List all possible rational roots. Then use a calculator, synthetic division and factoring to find all zeros & write in factored form (no fractions).

5.  $3x^4 + 19x^3 + 26x^2 - 16x - 32$

$C: 1, 32, 2, 16, 4, 8$   
 $L: 1, 3$

Possible Zeros (PRR):  $\pm 1, \pm \frac{1}{3}, \pm 32, \pm \frac{32}{3}, \pm 2, \pm \frac{2}{3}, \pm 16, \pm \frac{16}{3}, \pm 4, \pm \frac{4}{3}, \pm 8, \pm \frac{8}{3}$

SHOW WORK HERE:

$$1 \begin{array}{r|rrrrr} 3 & 19 & 26 & -16 & -32 \\ \downarrow & & & & & \\ 3 & 22 & 48 & 32 & 0 \\ \downarrow & & & & & \\ 3 & 16 & 16 & 0 & \\ \downarrow & & & & & \\ 3 & 4 & 0 & \end{array}$$

$3x + 4 = 0$   
 $3x = -4$   
 $x = -\frac{4}{3}$

Zeros:  $x = 1, x = -2, x = -4, x = -\frac{4}{3}$

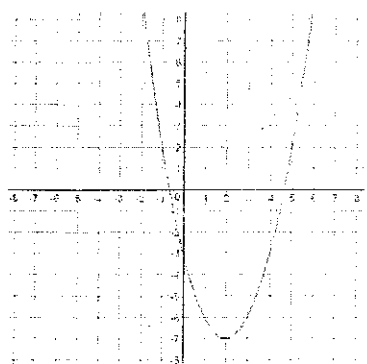
Factored Form:  $f(x) = (x-1)(x+2)(x+4)(3x+4)$

Given the following functions:

a.) State the number and type of zeros (# of real and/or # of imaginary). Find the discriminant when necessary.

b.) Use synthetic division to prove x-intercepts and find the remaining zeros (use quadratic formula when necessary).

6.  $f(x) = x^2 - 4x - 3$



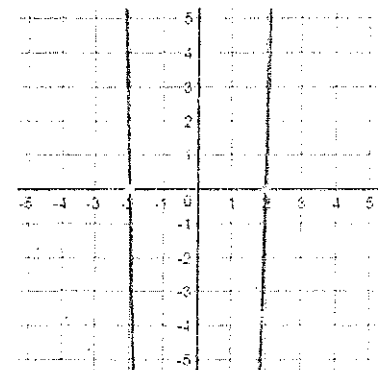
$a = 1$   
 $b = -4$   
 $c = -3$

Disc. =  $b^2 - 4ac$   
 $= (-4)^2 - 4(1)(-3)$   
 $= 28$

a.) # of Zeros: 2  
 Types of Zeros: 2 Real  
 Discriminant: 28  
 b.) Zeros:  $x = \frac{\sqrt{7}+2, -\sqrt{7}+2}{1}$   
 (include ALL zeros)

$x = \frac{-(-4) \pm \sqrt{28}}{2(1)}$   
 $x = \frac{4 \pm \sqrt{28}}{2} = \begin{cases} \sqrt{7}+2 \\ -\sqrt{7}+2 \end{cases}$

7.  $f(x) = x^4 + 3x^2 - 28$



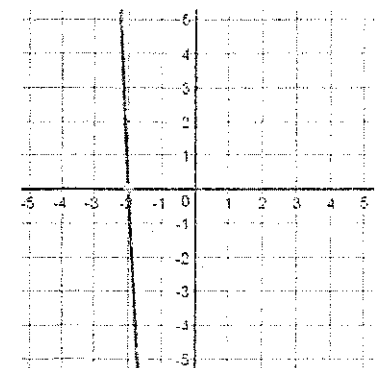
$-2 \mid 1 \ 0 \ 3 \ 0 \ -28$   
 $\downarrow -2 \ 4 \ -14 \ 28$   
 $2 \mid 1 \ -2 \ 7 \ -14 \ 0$   
 $\downarrow 2 \ 0 \ 14 \ 0$   
 $1 \ 0 \ 7 \ 0$   
 $x^2 \ x \ c$

$x = \frac{-(0) \pm \sqrt{(0)^2 - 4(1)(7)}}{2(1)}$   
 $x = \frac{0 \pm \sqrt{-28}}{2} = \pm i\sqrt{28}$

a.) # of Zeros: 4  
 Types of Zeros: 2 Real, 2 Imag.  
 Discriminant: n/a or -28  
 b.) Zeros:  $x = \frac{-2, 2, i\sqrt{7}, -i\sqrt{7}}{1}$   
 (include ALL zeros)

$x^2 + 7 = 0$   
 $x^2 = -7$   
 $x = \pm\sqrt{-7}$   
 $x = \pm i\sqrt{7}$

8.  $f(x) = -x^3 + 2x^2 - 16$



$-2 \mid -1 \ 2 \ 0 \ -16$   
 $\downarrow 2 \ -8 \ 16$   
 $-1 \ 4 \ -8 \ 0$   
 $a \ b \ c$

a.) # of Zeros: 3  
 Types of Zeros: 1 Real, 2 Imag.  
 Discriminant: -16  
 b.) Zeros:  $x = \frac{-2, 2-2i, 2+2i}{1}$   
 (include ALL zeros)

Disc =  $(4)^2 - 4(-1)(-8)$   
 $= -16$   
 $x = \frac{-(-4) \pm \sqrt{-16}}{2(-1)}$   
 $x = \frac{-4 \pm 4i}{-2} = \begin{cases} 2-2i \\ 2+2i \end{cases}$